

# Formelsammlung Trigonometrie

## Formules trigonométriques

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$$\sin^2 x + \cos^2 x = 1$$

$$\tan x = \frac{\sin x}{\cos x}$$

$$\cos^2 x = \frac{1}{1 + \tan^2 x}$$

$$\sin^2 x = \frac{\tan^2 x}{1 + \tan^2 x}$$

$$1 + \tan^2 x = \frac{1}{\cos^2 x}$$

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$$\sin(-x) = -\sin(x)$$

$$\sin(\pi - x) = \sin(x)$$

$$\sin(\pi + x) = -\sin(x)$$

$$\cos(-x) = \cos(x)$$

$$\cos(\pi - x) = -\cos(x)$$

$$\cos(\pi + x) = -\cos(x)$$

$$\tan(-x) = -\tan(x)$$

$$\tan(\pi - x) = -\tan(x)$$

$$\tan(\pi + x) = \tan(x)$$

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$$\sin\left(\frac{\pi}{2} - x\right) = \cos(x)$$

$$\sin\left(\frac{\pi}{2} + x\right) = \cos(x)$$

$$\cos\left(\frac{\pi}{2} - x\right) = \sin(x)$$

$$\cos\left(\frac{\pi}{2} + x\right) = -\sin(x)$$

$$\tan\left(\frac{\pi}{2} - x\right) = \cot(x)$$

$$\tan\left(\frac{\pi}{2} + x\right) = -\cot(x)$$

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$$\sin(x + y) = \sin x \cos y + \cos x \sin y$$

$$\tan(x + y) = \frac{\tan x + \tan y}{1 - \tan x \tan y}$$

$$\sin(x - y) = \sin x \cos y - \cos x \sin y$$

$$\cos(x + y) = \cos x \cos y - \sin x \sin y$$

$$\tan(x - y) = \frac{\tan x - \tan y}{1 + \tan x \tan y}$$

$$\cos(x - y) = \cos x \cos y + \sin x \sin y$$

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$$\sin 2x = 2 \sin x \cos x$$

$$2 \cos^2 x = 1 + \cos 2x$$

$$\cos 2x = \cos^2 x - \sin^2 x$$

$$2 \sin^2 x = 1 - \cos 2x$$

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$$\sin 2x = \frac{2 \tan x}{1 + \tan^2 x}$$

$$\cos 2x = \frac{1 - \tan^2 x}{1 + \tan^2 x}$$

$$\tan 2x = \frac{2 \tan x}{1 - \tan^2 x}$$

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$$\sin 3x = 3 \sin x - 4 \sin^3 x$$

$$\cos 3x = -3 \cos x + 4 \cos^3 x$$

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$$\sin x + \sin y = 2 \sin\left(\frac{x+y}{2}\right) \cos\left(\frac{x-y}{2}\right)$$

$$\tan x + \tan y = \frac{\sin(x+y)}{\cos x \cos y}$$

$$\sin x - \sin y = 2 \sin\left(\frac{x-y}{2}\right) \cos\left(\frac{x+y}{2}\right)$$

$$\tan x - \tan y = \frac{\sin(x-y)}{\cos x \cos y}$$

$$\cos x + \cos y = 2 \cos\left(\frac{x+y}{2}\right) \cos\left(\frac{x-y}{2}\right)$$

$$\cos x - \cos y = -2 \sin\left(\frac{x+y}{2}\right) \sin\left(\frac{x-y}{2}\right)$$

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$$\sin x \cos y = \frac{1}{2} [\sin(x+y) + \sin(x-y)]$$

$$\cos x \cos y = \frac{1}{2} [\cos(x+y) + \cos(x-y)]$$

$$\sin x \sin y = \frac{1}{2} [\cos(x-y) - \cos(x+y)]$$

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